

# Molecular constants and Rydberg–Klein–Rees (RKR) potential curve for the $\text{Na}_2 1^3\Sigma_g^-$ state

Yaoming Liu, Jian Li, Dieyan Chen, and Li Li<sup>a)</sup>

*Department of Physics and Center of Atomic Molecular Sciences, Tsinghua University, Beijing 100084, China*

Kevin M. Jones

*Department of Physics, Williams College, Williamstown, Massachusetts 01267*

Bing Ji<sup>b)</sup>

*Department of Chemistry, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

Robert J. Le Roy

*Guelph-Waterloo Centre for Graduate Work in Chemistry and Biochemistry, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada*

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Transitions into the doubly excited  $\text{Na}_2 1^3\Sigma_g^-$  state have been analyzed using near-dissociation expansions (NDE) to represent the vibrational energies and inertial rotational constants, while the centrifugal distortion constants were held fixed at “mechanically consistent” values calculated from the Rydberg–Klein–Rees (RKR) potential implied by those  $G(v)$  and  $B_v$  functions. The input data cover the range  $v=0$  to 57 and  $N$  up to 47, and the fit yields  $v_D=61.41(\pm 0.10)$  and  $D_0=3385.70(\pm 0.2)$   $\text{cm}^{-1}$ . © 1999 American Institute of Physics. [S0021-9606(99)01031-4]

In a previous publication, some of us reported an experimental and theoretical study of the  $1^3\Sigma_g^-$  state of  $\text{Na}_2$ .<sup>1</sup> More than 400 transitions from the  $b^3\Pi_u$  state into the  $v=0-57$ ,  $N=2-24$  levels of the  $1^3\Sigma_g^-$  state were observed by perturbation facilitated optical–optical double resonance (PFOODR) fluorescence excitation spectroscopy, and molecular constants were reported. Unfortunately, only a simple Dunham fit was performed and mechanically consistent centrifugal distortion constants were not incorporated into that analysis. In earlier work, using two-step polarization labeling spectroscopy, Jones *et al.*<sup>2,3</sup> observed 180 transitions from the  $b^3\Pi_u$  state into a  $\text{Na}_2$  triplet gerade state, which was tentatively assigned as the  $3s+4d^3\Pi_g$  state, but later recognized to be the  $1^3\Sigma_g^-$  state.<sup>1</sup> The vibrational levels observed by Jones *et al.* range from  $v=3-28$  and the rotational levels include the high- $N$  values of 43, 45, and 47. In both sets of measurements, the line position uncertainty was typically  $0.2 \text{ cm}^{-1}$  except for the very highest levels ( $v>53$ ), where the calibration lines were not close and the uncertainties are considerably larger.

The present work reanalyzed the combined PFOODR fluorescence excitation and two-step polarization labeling data sets using near-dissociation expansion (NDE) expressions for the vibrational energies and inertial rotational constants. Since the molecular constants for the ground and intermediate states are well-known,<sup>4,5</sup> the experimental data were converted into a set of final-state level energies, expressed relative to the ground electronic state potential mini-

mum. The fitting procedure was then applied to this set of final-state term values.<sup>6</sup>

For vibrational levels lying close to dissociation, the characteristic behavior of the energies, rotational constants, and other properties of a diatomic molecule are defined by the nature of the asymptotically dominant attractive inverse-power term in the long-range internuclear potential

$$E(R) \approx D - \frac{C_n}{R^n}, \quad (1)$$

where  $D$  is the dissociation energy and  $C_n$  the leading long-range potential coefficient.<sup>7-11</sup> Use of NDE expressions for vibrational energies and rotational constants, which incorporate the theoretically predicted limiting near-dissociation behavior implied by Eq. (1),<sup>7-9,11</sup> yields both compact representations of the data to which it was fitted, and reliable extrapolations for those and other properties.<sup>12-15</sup> They also yield particularly compact and reliable expressions for representing very large data sets spanning a large fraction of a potential energy well.<sup>16-18</sup> This approach is therefore used here to describe the  $1^3\Sigma_g^-$  state of  $\text{Na}_2$ .

The NDE expression for the vibrational energies used in the present work has the form

$$G_v = D - X_0(n)(v_D - v)^{2n/(n-2)}[L/M], \quad (2)$$

where  $v_D$  is the effective vibrational index at dissociation (which usually is noninteger),  $X_k(n) = \bar{X}_k(n)/[\mu^n(C_n)^2]^{1/(n-2)}$ ,  $\mu$  is the diatom reduced mass (in amu), and  $\bar{X}_k(n)$  is a known numerical factor depending only on the physical constants and the value of the integer  $n$ ,<sup>7,8,19</sup> and  $[L/M]$  is a rational polynomial with orders  $L$  and  $M$

<sup>a)</sup> Author to whom all correspondence should be addressed. Electronic mail: lili@lsad.tsinghua.edu.cn

<sup>b)</sup> Present address: Air Products and Chemicals, Inc., Allentown, PA 18195.

$$[L/M] = \frac{1 + \sum_{i=1}^L p_i^0 (v_D - v)^i}{1 + \sum_{i=1}^M q_i (v_D - v)^i} \quad (3)$$

The NDE expression used for the inertial rotational constants is

$$B_v = X_1(n) (v_D - v)^{2n/(n-2)} \exp \left[ \sum_{i=1}^L p_i^1 (v_D - v)^i \right], \quad (4)$$

where  $X_1(n)$  is defined above [with<sup>19</sup>  $\bar{X}_0(6) = 7932.0$  and  $\bar{X}_1(6) = 546.64$ ]. Computer programs GvNDE and ExpNDE for performing (nonlinear) least-squares fits to Eqs. (2) and (4), respectively, may be obtained from one of us (RJL) on request.<sup>20</sup> While a number of other types of expansions have sometimes been used for the vibrational energies, including an exponential expansion analogous to Eq. (4),<sup>15,16</sup> in our experience mixed numerator/denominator rational polynomials of the type shown in Eq. (3) usually yield the best fits for a given number of parameters. For a given total number of vibrational expansion parameters, GvNDE automatically performs fits to a variety of different expansions, which facilitates the choice of the most compact and accurate NDE form for a given case. While other choices would do nearly as well, a [3,2] “outer expansion” based on Eqs. (2) and (3) was chosen here.

According to theory, the 0<sub>g</sub><sup>+</sup> and the 1<sub>g</sub> components of the 1<sup>3</sup>Σ<sub>g</sub><sup>-</sup> state dissociate to the  $P_{1/2} + P_{1/2}$  and  $P_{1/2} + P_{3/2}$  atomic limits, respectively,<sup>21,22</sup> and  $n = 6$  is the power of the dominant term in the long-range interaction potential for  $R > 20$  bohr.<sup>21</sup> The theoretical value of the coefficient  $C_6$  is  $2.0578 \times 10^7 \text{ cm}^{-1} \text{ \AA}^6$ ,<sup>21-24</sup> in our NDE fits,  $C_6$  is fixed at this value. The dissociation limit of this state, defined as the sum of the dissociation energy for the ground  $X^1\Sigma_g^+$  state of Na<sub>2</sub> determined by Jones *et al.*,<sup>25</sup>  $D_e = 6022.0186$  ( $\pm 0.0053$ ) cm<sup>-1</sup>, plus the known<sup>26</sup>  $^2P_{1/2}$  and  $^2P_{3/2}$  atomic excitation energies, is a more accurate value than can be determined from the present data. The present analysis therefore fixed this limit at that value,  $D(\text{limit}) = 39\,951.591 \text{ cm}^{-1}$ , expressed relative to the ground-state potential minimum.

The present analysis procedure consists of the following steps:

- (1) Determine initial estimates of  $G_v$  and  $B_v$  for the observed levels from band-by-band fits to the raw experimental data;
- (2) Use the GvNDE and ExpNDE codes<sup>20</sup> to fit the sets of individual  $G_v$  and  $B_v$  values to Eqs. (2) and (4), respectively, to obtain preliminary estimates of  $v_D$  and of the form and parameters  $\{p_i^j\}$  and  $\{q_i\}$  of the empirical expansions in Eqs. (2)–(4);
- (3) Calculate an RKR potential energy curve from those NDE expansions using the program RKR1;<sup>20,27</sup>
- (4) Use the program LEVEL<sup>20,28</sup> to calculate the centrifugal distortion constants (up to  $O_v$ ) for the observed vibrational levels, from the RKR potential obtained in step (3);
- (5) Subtracting the contributions of the centrifugal distortion constants determined in step (4), use the program DSPARFIT<sup>20,29</sup> to refit the raw experimental data to deter-

TABLE I. Parameters defining the NDE functions determined for the vibrational energies and  $B_v$  constants of the 1<sup>3</sup>Σ<sub>g</sub><sup>-</sup> state of Na<sub>2</sub>, obtained with  $C_6 = 2.057\,74 \times 10^7 \text{ cm}^{-1} \text{ \AA}^6$ ,  $v_D = 61.41(\pm 0.10)$  and  $D(\text{limit}) = 39\,951.591 \text{ cm}^{-1}$  (relative to the ground-state potential minimum). This recommended vibrational expansion implies  $D_0(1^3\Sigma_g^-) = 3385.70$  ( $\pm 0.2$ ) cm<sup>-1</sup>,  $D_e(1^3\Sigma_g^-) = 3432.46(\pm 0.2) \text{ cm}^{-1}$ , and  $T_e = 36\,519.13$  ( $\pm 0.2$ ) cm<sup>-1</sup>.

	$G(v)=[j=0]$	$B_v[j=1]$
$X_j(6)/\text{cm}^{-1}$	$4.4867 \times 10^{-2}$	$3.0921 \times 10^{-3}$
$p_1^j$	0.436 636	0.1341
$p_2^j$	$-3.529 \times 10^{-3}$	$-1.6863 \times 10^{-2}$
$p_3^j$	$1.54 \times 10^{-5}$	$9.2 \times 10^{-4}$
$p_4^j$	...	$-2.810\,837 \times 10^{-5}$
$p_5^j$	...	$4.924 \times 10^{-7}$
$p_6^j$	...	$-4.619\,52 \times 10^{-9}$
$p_7^j$	...	$-1.8 \times 10^{-11}$
$q_1$	$4.8 \times 10^{-2}$	...
$q_2$	$1.366 \times 10^{-2}$	...

mine refined values of  $v_D$  and of the  $\{p_i^j\}$  and  $\{q_i\}$  parameters defining the NDE functions for  $G(v)$  and  $B_v$ ;

(6) Repeat steps (3)–(5) until convergence is achieved. When this occurs, the  $v_D$  value was rounded at the second digit of its uncertainty and the fit repeated while applying the sequential rounding and refitting procedure of Ref. 30. This had no effect on the quality of the fit to the experimental data.

The final NDE expansion parameters determined in this way are given in Table I, while the associated calculated values for the first three centrifugal distortion constants are listed in Table II; while higher-order distortion constants were also computed, their effect is much smaller than the uncertainties in the data. The reduced precision for the  $B_v$  values for levels above  $v = 28$  listed in Table II reflects the fact that data for the lower levels involve rotational sublevels up to  $N = 47$ , while those for the higher vibrational levels are restricted to  $N < 25$ . The final fit had a dimensionless standard error<sup>30</sup> of  $\bar{\sigma}_f = 1.04$ , which means that on average the differences between the calculated and observed term values are within (only 4% larger than) the estimated experimental uncertainties of ca. 0.2 cm<sup>-1</sup>. In contrast, predictions yielded by the Dunham constants reported in Ref. 1 yielded  $\bar{\sigma}_f = 1.99$  for this data set.

The values and derivatives of our NDE expressions for  $G(v)$  and  $B_v$  at  $v = -1/2$  also yield improved estimates of the conventional spectroscopic parameters:  $\omega_e = 93.74$  ( $\pm 0.05$ ),  $\omega_e x_e = 0.452(\pm 0.016)$ ,  $B_e = 0.1183(\pm 0.0010)$ , and  $\alpha_e = 1.9(\pm 0.5) \times 10^{-3} \text{ cm}^{-1}$ , whose uncertainties are fully correlated values generated from the results of the fit using Eq. (7) of Ref. 30. These constants in turn yield  $R_e = 3.520(\pm 0.015) \text{ \AA}$  and  $Y_{00} = 0.171 \text{ cm}^{-1}$ . The size of this  $Y_{00}$  value indicates that higher-order terms in the semiclassical quantization condition are relatively large for this rather anharmonic potential. This was approximately taken into account by our use of the Kaiser correction (integration from  $v = -1/2 - Y_{00}/\omega_e$ ) (Ref. 31) in the RKR calculation to determine the potential function from which the centrifugal dis-

TABLE II. Band constants (in  $\text{cm}^{-1}$ ) and turning points (in  $\text{\AA}$ ) of the  $1^3\Sigma_g^-$  state of  $\text{Na}_2$  yielded by the present analysis.

$v$	$G_v$	$B_v$	$D_v$	$H_v$	$L_v$	$R_1(v)$	$R_2(v)$
0	0.00	0.117 477	$7.42 \times 10^{-7}$	$1.21 \times 10^{-12}$	$2.55 \times 10^{-17}$	3.356	3.711
1	92.75	0.115 957	$7.22 \times 10^{-7}$	$3.70 \times 10^{-12}$	$-6.90 \times 10^{-17}$	3.250	3.867
2	184.65	0.114 701	$7.14 \times 10^{-7}$	$5.31 \times 10^{-12}$	$-1.14 \times 10^{-16}$	3.182	3.981
3	275.68	0.113 633	$7.14 \times 10^{-7}$	$6.20 \times 10^{-12}$	$-1.22 \times 10^{-16}$	3.128	4.077
4	365.83	0.112 692	$7.18 \times 10^{-7}$	$6.53 \times 10^{-12}$	$-1.07 \times 10^{-16}$	3.082	4.163
5	455.09	0.111 830	$7.23 \times 10^{-7}$	$6.45 \times 10^{-12}$	$-7.88 \times 10^{-17}$	3.042	4.242
6	543.46	0.111 011	$7.28 \times 10^{-7}$	$6.10 \times 10^{-12}$	$-4.73 \times 10^{-17}$	3.006	4.316
7	630.93	0.110 209	$7.32 \times 10^{-7}$	$5.60 \times 10^{-12}$	$-1.89 \times 10^{-17}$	2.973	4.386
8	717.48	0.109 406	$7.36 \times 10^{-7}$	$5.04 \times 10^{-12}$	$2.13 \times 10^{-18}$	2.943	4.454
9	803.13	0.108 591	$7.38 \times 10^{-7}$	$4.51 \times 10^{-12}$	$1.32 \times 10^{-17}$	2.915	4.519
10	887.85	0.107 757	$7.39 \times 10^{-7}$	$4.05 \times 10^{-12}$	$1.34 \times 10^{-17}$	2.889	4.583
11	971.64	0.106 901	$7.39 \times 10^{-7}$	$3.69 \times 10^{-12}$	$3.09 \times 10^{-18}$	2.865	4.646
12	1054.49	0.106 021	$7.39 \times 10^{-7}$	$3.46 \times 10^{-12}$	$-1.58 \times 10^{-17}$	2.842	4.708
13	1136.39	0.105 118	$7.39 \times 10^{-7}$	$3.35 \times 10^{-12}$	$-4.06 \times 10^{-17}$	2.821	4.769
14	1217.32	0.104 195	$7.39 \times 10^{-7}$	$3.35 \times 10^{-12}$	$-6.79 \times 10^{-17}$	2.801	4.830
15	1297.29	0.103 252	$7.40 \times 10^{-7}$	$3.44 \times 10^{-12}$	$-9.44 \times 10^{-17}$	2.782	4.890
16	1376.26	0.102 291	$7.42 \times 10^{-7}$	$3.58 \times 10^{-12}$	$-1.16 \times 10^{-16}$	2.764	4.950
17	1454.24	0.101 314	$7.44 \times 10^{-7}$	$3.74 \times 10^{-12}$	$-1.31 \times 10^{-16}$	2.747	5.010
18	1531.19	0.100 322	$7.48 \times 10^{-7}$	$3.88 \times 10^{-12}$	$-1.35 \times 10^{-16}$	2.731	5.069
19	1607.11	0.099 314	$7.52 \times 10^{-7}$	$3.96 \times 10^{-12}$	$-1.27 \times 10^{-16}$	2.716	5.129
20	1681.96	0.098 289	$7.58 \times 10^{-7}$	$3.94 \times 10^{-12}$	$-1.06 \times 10^{-16}$	2.701	5.190
21	1755.75	0.097 248	$7.64 \times 10^{-7}$	$3.81 \times 10^{-12}$	$-7.29 \times 10^{-17}$	2.687	5.250
22	1828.43	0.096 187	$7.71 \times 10^{-7}$	$3.53 \times 10^{-12}$	$-2.85 \times 10^{-17}$	2.674	5.311
23	1899.98	0.095 104	$7.78 \times 10^{-7}$	$3.10 \times 10^{-12}$	$2.33 \times 10^{-17}$	2.661	5.373
24	1970.39	0.093 997	$7.86 \times 10^{-7}$	$2.52 \times 10^{-12}$	$7.80 \times 10^{-17}$	2.648	5.435
25	2039.63	0.092 863	$7.93 \times 10^{-7}$	$1.81 \times 10^{-12}$	$1.30 \times 10^{-16}$	2.636	5.497
26	2107.65	0.091 699	$8.01 \times 10^{-7}$	$9.96 \times 10^{-13}$	$1.73 \times 10^{-16}$	2.625	5.561
27	2174.45	0.090 502	$8.09 \times 10^{-7}$	$1.06 \times 10^{-13}$	$2.02 \times 10^{-16}$	2.614	5.626
28	2239.97	0.089 269	$8.17 \times 10^{-7}$	$-8.15 \times 10^{-13}$	$2.12 \times 10^{-16}$	2.604	5.692
29	2304.20	0.088 00	$8.26 \times 10^{-7}$	$-1.73 \times 10^{-12}$	$2.01 \times 10^{-16}$	2.594	5.759
30	2367.09	0.086 69	$8.35 \times 10^{-7}$	$-2.61 \times 10^{-12}$	$1.68 \times 10^{-16}$	2.584	5.828
31	2428.61	0.085 34	$8.45 \times 10^{-7}$	$-3.42 \times 10^{-12}$	$1.15 \times 10^{-16}$	2.575	5.899
32	2488.72	0.083 94	$8.56 \times 10^{-7}$	$-4.15 \times 10^{-12}$	$4.42 \times 10^{-17}$	2.566	5.971
33	2547.38	0.082 50	$8.69 \times 10^{-7}$	$-4.83 \times 10^{-12}$	$-4.01 \times 10^{-17}$	2.558	6.045
34	2604.56	0.081 01	$8.83 \times 10^{-7}$	$-5.48 \times 10^{-12}$	$-1.34 \times 10^{-16}$	2.550	6.122
35	2660.21	0.079 47	$8.99 \times 10^{-7}$	$-6.14 \times 10^{-12}$	$-2.31 \times 10^{-16}$	2.542	6.201
36	2714.28	0.077 88	$9.18 \times 10^{-7}$	$-6.84 \times 10^{-12}$	$-3.16 \times 10^{-16}$	2.535	6.283
37	2766.74	0.076 23	$9.40 \times 10^{-7}$	$-7.56 \times 10^{-12}$	$-3.95 \times 10^{-16}$	2.528	6.368
38	2817.52	0.074 53	$9.65 \times 10^{-7}$	$-8.42 \times 10^{-12}$	$-4.84 \times 10^{-16}$	2.521	6.457
39	2866.58	0.072 76	$9.93 \times 10^{-7}$	$-9.49 \times 10^{-16}$	$-5.61 \times 10^{-16}$	2.515	6.549
40	2913.87	0.070 93	$1.03 \times 10^{-6}$	$-1.08 \times 10^{-11}$	$-6.38 \times 10^{-16}$	2.509	6.646
41	2959.32	0.069 02	$1.06 \times 10^{-6}$	$-1.24 \times 10^{-11}$	$-7.42 \times 10^{-16}$	2.503	6.748
42	3002.88	0.067 04	$1.10 \times 10^{-6}$	$-1.44 \times 10^{-11}$	$-8.44 \times 10^{-16}$	2.498	6.855
43	3044.48	0.064 97	$1.15 \times 10^{-6}$	$-1.69 \times 10^{-11}$	$-1.01 \times 10^{-15}$	2.493	6.969
44	3084.05	0.062 81	$1.21 \times 10^{-6}$	$-2.01 \times 10^{-11}$	$-1.20 \times 10^{-15}$	2.488	7.090
45	3121.53	0.060 55	$1.27 \times 10^{-6}$	$-2.41 \times 10^{-11}$	$-1.50 \times 10^{-15}$	2.484	7.220
46	3156.82	0.058 18	$1.34 \times 10^{-6}$	$-2.92 \times 10^{-11}$	$-1.91 \times 10^{-15}$	2.480	7.359
47	3189.87	0.055 68	$1.43 \times 10^{-6}$	$-3.57 \times 10^{-11}$	$-2.50 \times 10^{-15}$	2.476	7.511
48	3220.57	0.053 04	$1.52 \times 10^{-6}$	$-4.41 \times 10^{-11}$	$-3.38 \times 10^{-15}$	2.473	7.678
49	3248.84	0.050 24	$1.64 \times 10^{-6}$	$-5.51 \times 10^{-11}$	$-4.66 \times 10^{-15}$	2.469	7.862
50	3274.60	0.047 28	$1.78 \times 10^{-6}$	$-6.98 \times 10^{-11}$	$-6.65 \times 10^{-15}$	2.466	8.068
51	3297.73	0.044 11	$1.95 \times 10^{-6}$	$-8.98 \times 10^{-11}$	$-9.84 \times 10^{-15}$	2.464	8.302
52	3318.17	0.040 74	$2.15 \times 10^{-6}$	$-1.18 \times 10^{-10}$	$-1.52 \times 10^{-15}$	2.462	8.572
53	3335.83	0.037 13	$2.39 \times 10^{-6}$	$-1.59 \times 10^{-10}$	$-2.47 \times 10^{-15}$	2.460	8.891
54	3350.65	0.033 27	$2.70 \times 10^{-6}$	$-2.21 \times 10^{-10}$	$-4.34 \times 10^{-15}$	2.458	9.276
55	3362.62	0.029 16	$3.08 \times 10^{-6}$	$-3.26 \times 10^{-10}$	$-8.52 \times 10^{-15}$	2.457	9.756
56	3371.79	0.024 81	$3.58 \times 10^{-6}$	$-5.16 \times 10^{-10}$	$-1.87 \times 10^{-13}$	2.456	10.381
57	3378.32	0.020 28	$4.23 \times 10^{-6}$	$-8.97 \times 10^{-10}$	$-5.61 \times 10^{-13}$	2.455	11.239

tortion constants were calculated. However, this correction is only a first approximation to the treatment of higher-order semiclassical terms, so one may expect to find (see below) small discrepancies between quantal eigenvalues and  $B_v$ 's

calculated on this semiclassical potential and the values defined by the NDE functions used as input to the RKR calculation.

Values of band constants calculated<sup>28</sup> from the RKR po-

tential generated<sup>27</sup> from these NDE expansions, together with rounded values of the RKR turning points themselves, are listed in Table II. More precise RKR points may be readily generated from our  $G(v)$  and  $B_v$  expansions using standard programs,<sup>20,27</sup> and a listing appropriate for computational applications is available on request.<sup>6</sup> The  $G(v)$  and  $B_v$  values listed in Table II differ slightly from those implied by our NDE expansions because of two minor sources of inconsistency in the iterative procedure described above. The first is the fact that while the tabulated band constants were obtained by performing a quantal calculation on the RKR potential, the RKR inversion procedure is based on the first-order semiclassical or Jeffreys–Wentzel–Kramers–Brillouin (JWKB) approximation. The second is the fact that because of uncertainties in the experimental  $B_v$  determination, the inner-wall RKR turning points must be smoothed (here, for  $v > 34$ ) in order to prevent anomalous “wiggling” of the inner potential wall, and this smoothing implicitly changes the  $B_v$  values for levels above its onset. The program RKR1 performs such inner-wall smoothing (and the associated outer turning point adjustment<sup>28</sup>) by extrapolating above a given (user-selected) point with an exponential fitted to the preceding three inner turning points; the maximum resulting turning point shift was only ca. 0.01 Å. Moreover, below the onset of the inner-wall smoothing, the discrepancies in the  $B_v$  values were typically less than 0.01%, while those associated with the vibrational spacings are typically less than  $0.02 \text{ cm}^{-1}$ , so quantal/semiclassical discrepancies are significantly less than our experimental uncertainties. In any case, predictions of the data generated from the (quantal) calculated band constants of Table II are essentially identical (within the uncertainties) to those implied by the  $G(v)$  and  $B_v$  expansions of Table I (and the centrifugal distortion constants of Table II), so these potential sources of inconsistency have no significant effect on the present analysis.

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- <sup>1</sup>Y. Liu, J. Li, M. Xue, D. Chen, Li Li, and G.-H. Jeung, *J. Chem. Phys.* **103**, 7213 (1995), and references therein. In Ref. 1 there is a typographical error in Table I where the experimental  $R_e$  value calculated from  $B_e$  should be 3.511 Å, rather than 3.543 Å.
- <sup>2</sup>K. M. Jones, Ph.D. thesis, Stanford University, Stanford, California (1983).
- <sup>3</sup>K. M. Jones, E. J. Bredford, and A. L. Schawlow (unpublished).
- <sup>4</sup>P. Kusch and M. M. Hessel, *J. Chem. Phys.* **68**, 2591 (1978).
- <sup>5</sup>T.-J. Whang, W. C. Stwalley, Li Li, and A. M. Lyyra, *J. Chem. Phys.* **97**, 7211 (1992), and references therein.
- <sup>6</sup>See AIP Document No. EPAPS E-JCPSA6-111-010931 for raw data and RKR potential energy curve of the ( $\text{Na}_2$   $1^3\Sigma_g^-$  state). EPAPS document files may be retrieved free of charge from AIP's FTP server (<http://www.aip.org/pubservs/paps.html>) or from <ftp.aip.org> in the directory /epaps/. For further information, e-mail: [paps@aip.org](mailto:paps@aip.org) or fax: 516-576-2223. The raw data and RKR potential curve can also be obtained by sending a request via electronic mail to [lili@lsad.tsinghua.edu.cn](mailto:lili@lsad.tsinghua.edu.cn)
- <sup>7</sup>R. J. Le Roy and R. B. Bernstein, *Chem. Phys. Lett.* **5**, 42 (1970).
- <sup>8</sup>R. J. Le Roy and R. B. Bernstein, *J. Chem. Phys.* **52**, 3869 (1970).
- <sup>9</sup>W. C. Stwalley, *Chem. Phys. Lett.* **6**, 241 (1970).
- <sup>10</sup>W. C. Stwalley, *J. Chem. Phys.* **58**, 3867 (1973).
- <sup>11</sup>R. J. Le Roy and M. G. Barwell, *Can. J. Phys.* **53**, 1983 (1975).
- <sup>12</sup>A.-R. Hashemi-Attar, C. L. Beckel, W. N. Keepin, and S. A. Sonnenleitner, *J. Chem. Phys.* **70**, 3881 (1979).
- <sup>13</sup>R. J. Le Roy and W.-H. Lam, *Chem. Phys. Lett.* **71**, 544 (1980).
- <sup>14</sup>J. W. Tromp and R. J. Le Roy, *Can. J. Phys.* **60**, 26 (1982).
- <sup>15</sup>R. J. Le Roy, *J. Chem. Phys.* **101**, 10217 (1994).
- <sup>16</sup>J. W. Tromp and R. J. Le Roy, *J. Mol. Spectrosc.* **109**, 352 (1985).
- <sup>17</sup>B. Ji, C. Tsai, Li Li, T. Whang, A. M. Lyyra, H. Wang, J. Bahns, W. C. Stwalley, and R. J. Le Roy, *J. Chem. Phys.* **103**, 7240 (1995).
- <sup>18</sup>D. R. T. Appadoo, R. J. Le Roy, P. F. Bernath, S. Gerstenkorn, P. Luc, J. Verges, J. Sinzelle, J. Chevillard, and Y. D'Aignaux, *J. Chem. Phys.* **104**, 903 (1996).
- <sup>19</sup>R. J. Le Roy, in *Semiclassical Methods in Molecular Scattering and Spectroscopy*, edited by M. S. Child (Reidel, Dordrecht, 1980), p. 109.
- <sup>20</sup>This program may be obtained from R. J. Le Roy by sending a request via electronic mail to [leroy@uwaterloo.ca](mailto:leroy@uwaterloo.ca)
- <sup>21</sup>T. Y. Chang, *Rev. Mod. Phys.* **39**, 911 (1967).
- <sup>22</sup>R. W. Heather and P. S. Julienne, *Phys. Rev. A* **47**, 1887 (1993).
- <sup>23</sup>M. Merawa and M. Rerat, *J. Chem. Phys.* **106**, 3658 (1997).
- <sup>24</sup>M. Marinescu, *Phys. Rev. A* **56**, 4764 (1997).
- <sup>25</sup>K. M. Jones, S. Maleki, S. Bize, P. D. Lett, C. J. Williams, H. Richling, H. Knockel, E. Tiemann, H. Wang, P. L. Gould, and W. C. Stwalley, *Phys. Rev. A* **54**, R1006 (1996).
- <sup>26</sup>C. E. Moore, *Atomic Energy Levels as Derived from the Analysis of Atomic Spectra*, Vol. 1 (National Bureau of Standards, U.S. Department of Commerce, Washington, 1949).
- <sup>27</sup>R. J. Le Roy, RKR1: A Computer Program Implementing the First-Order RKR Method for Determining Diatom Potential Energy Curves from Spectroscopic Constants (University of Waterloo, Chemical Physics Research Report, 1992) (Ref. 18).
- <sup>28</sup>R. J. Le Roy, LEVEL 6.1: A Computer Program Solving the Radial Schrödinger Equation for Bound and Quasibound Levels, and Calculating Various Expectation Values and Matrix Elements (University of Waterloo, Chemical Physics Research Report, 1996) (Ref. 20).
- <sup>29</sup>R. J. Le Roy, *J. Mol. Spectrosc.* **194**, 189 (1999).
- <sup>30</sup>R. J. Le Roy, *J. Mol. Spectrosc.* **191**, 223 (1998).
- <sup>31</sup>E. W. Kaiser, *J. Chem. Phys.* **53**, 1686 (1978).

**ERRATA****Erratum: “Molecular constants and Rydberg–Klein–Rees (RKR) potential curve for the Na<sub>2</sub> 1<sup>3</sup>Σ<sub>g</sub><sup>-</sup> state” [J. Chem. Phys. 111, 3494 (1999)]**

Yaoming Liu, Jian Li, Dieyan Chen, and Li Li

*Department of Modern Applied Physics and Center of Atomic Molecular Sciences, Tsinghua University, Beijing 100084, China*

Kevin M. Jones

*Department of Physics, Williams College, Williamstown, Massachusetts 01267*

Bing Ji

*Department of Chemistry, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

Robert J. Le Roy

*Guelph-Waterloo Centre for Graduate Work in Chemistry and Biochemistry, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada*

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The power in Eq. (4) is incorrect. The near-dissociation expansion expression for the inertial rotational constant should read

$$B_v = X_1(n)(v_D - v)^{4/(n-2)} \exp \left[ \sum_{i=1}^L p_i^1 (v_D - v)^i \right]. \quad (4)$$

We are grateful to Dr. Claude Amiot for bringing this error to our attention.

## Erratum: "Molecular constants and Rydberg–Klein–Rees (RKR) potential curve for the $\text{Na}_2 1^3\Sigma_g^-$ state" [J. Chem. Phys. 111, 3494 (1999)]

Yaoming Liu, Jian Li, Dieyan Chen, and Li Li

*Department of Physics and Center of Atomic Molecular Sciences, Tsinghua University, Beijing 100084, China*

Kevin M. Jones

*Department of Physics, Williams College, Williamstown, Massachusetts 01267*

Bing Ji

*Department of Chemistry, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

Robert J. Le Roy

*Guelph-Waterloo Centre for Graduate Work in Chemistry and Biochemistry, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada*

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The final parameter in the exponential NDE expansion for  $B_v$  in Table I was shown with the wrong sign; it should be  $p_7^1 = +1.8 \times 10^{-11}$ . As noted previously,<sup>1</sup> the NDE expression for  $B_v$  in Eq. (4) should have read  $B_v = X_1(n) \times (v_{\infty} - v)^{4/(n-2)} \exp(\sum_{i=1}^L p_i^1 (v_{\infty} - v)^i)$ .

<sup>1</sup>Y. Liu, J. Li, D. Chen, L. Li, K. M. Jones, B. Ji, and R. J. Le Roy, J. Chem. Phys. **117**, 6380 (2002).